An Analysis of Frieze Patterns, Crystallographic Patterns, and Philosophical Values on Subahnale Woven Motifs Sukarare Village

Lalu Muhammad Fauzi¹, Shahibul Ahyan², Sri Supiyati³, Nila Hayati⁴, Rodysatriawan⁵

Mathematics Education Study Program, Hamzanwadi University
Jalan TGKH Muhammad Zainuddin Abdul Majid, No. 132, NTB, Indonesia
¹lmfauzi@hamzanwadi.ac.id; ²shahirulahyan@hamzanwadi.ac.id; ³sri.supiyati@hamzanwadi.ac.id; ⁴hayatisyahdani@hamzanwadi.ac.id; ⁵rodysatriawan@hamzanwadi.ac.id

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Abstract
Culture, with its diversity and unique customs, arts, and crafts, provides an identity for a region. This cultural uniqueness can be studied as part of learning resources. Ethnomathematics is a bridge to exploring mathematics that develops in society. Thus, this study seeks to analyze the frieze patterns, crystallographic patterns, and philosophical values in the subahnale woven fabric motifs in Sukarare Village. The method used in this research is the ethnographic method. Research data were collected through observation, literature study, and interviews with cultural practitioners, traditional leaders, woven cloth artisans, and humanists. The results showed that the motif (reragian) of the subahnale woven fabric was formed by a combination of geometric shapes: lines, triangles, rectangles, and hexagons. The geometric shapes are arranged using a mathematical model: translation, rotation, and reflection. The patterns formed are 4 frieze patterns, namely patterns 3, 4, 6, and 7. In addition, there are also crystallographic patterns, namely patterns p1, pm, and p4m.

Keywords: philosophical; frieze; Woven Fabrics; crystallography.
I. INTRODUCTION

Travel and notes on the emergence and presence of something is an event. When the process gives rise to an event that developed before then, we are faced with a history (Nemeth, 2016). When dealing with a phenomenon, cultural groups try to respond and seek explanations about that phenomenon in unique ways and techniques. This kind of activity is the origin of human knowledge. In responding to their environment, a group of cultures in each region in patterns and styles are found as part of building a knowledge system (D'Ambrosio, 2016; Rosa & Orey, 2016). The activity of comparing, classifying, evaluating, quantifying, measuring, and calculating through observation tries to explain and understand the knowledge of that culture (Rosa & Orey, 2016).

Cultural diversity with all forms of customs as part of historical heritage provides opportunities for improving the education system, which is the mathematics education system which seeks to bring the realities of life and culture closer through ethnomathematics (Abdullah, 2017). Cultural identity positively reflects a society's equality and socio-cultural level. Originality and uniqueness reflected in various activities, artifacts, and customs in culture can be used as a source of mathematics, including the culture of the Sasak people (Fauzi et al., 2021; Fauzi, Hanum, et al., 2022; Fauzi & Gazali, 2022). Community activities in culture are seen as mere habits and contain historical and philosophical values that impact student character building, such as diligence, conscientiousness, economical, mutual respect, and social spirit (Widodo, 2019; Hartono & Putra, 2022).

The Sasak people still maintain traditions and ancestral customs. Various remains in the form of artifacts, such as traditional villages and traditional arts and crafts, are still being preserved. One of them is conventional crafts in the form of traditional woven fabrics, which can be explored in learning mathematics. Several researchers have begun to look at the cultural uniqueness of the Sasak people through ethnomathematics studies, including (Fauzi, Hayati, et al., 2022; Fauzi & Gazali, 2022; Fitriyah & Syafi'i, 2022; Hardiani & Putrawangsa, 2019; Novitasari et al., 2022). Fauzi, Hayati, et al. (2022) conducted a study of the exploration of mathematics and cultural values in the perisian performing arts, Fauzi and Gazali (2022) ethnomathematics studies of residential characteristics based on crew elbows, Fitriyah and Syafi'i, (2022) examines the ethnomathematics contained in the bale lumbung, Hardiani and Putrawangsa (2019) Ethnomathematics: The tradition of measuring the Sasak people and its integration potential in mathematics learning and Novitasari et al. (2022) conducted an ethnomathematics study of mathematical exploration of the gendang beleq art (Iqrima, Zulkarnain, & Kamaliyah, 2023).
In addition, several researchers conducted an exploratory study of the geometry of the traditional woven fabrics of the Sasak people, as was done by Fauzi et al. (2023) with a survey of geometric perceptions and cultural values on traditional woven cloth motifs for the Sasak people, Sutarto et al. (2021) an exploration of the geometric transformation of the weaving geometry of the Sasak Sukarara tribe, Fauzi and Setiawan (2020) conducted a study on ethnomathematics: The concept of geometry in traditional Sasak crafts in teaching mathematics in elementary schools. From the studies described above, no researcher has yet conducted a study to look at the frieze patterns, crystallographic patterns, and philosophical values of the subahnale woven fabric motifs in Sukarare Village. Various motifs are found on subahnale woven fabrics. Every motif or design in woven fabrics is related to aesthetics and contains local values. This provides an overview of spiritual, historical, and metaphysical principles, which can be felt, expressed, and applied in daily life.

The motifs or reragian found on the traditional woven fabrics of the Sasak people generally use geometric patterns such as rectangles, squares, triangles, and other shapes. These geometric patterns are often found in mathematics learning related to frieze and crystallographic patterns.

Frieze patterns or groups are symmetrical groups built by one-way translations to form a repeating linear pattern (Cooper, 2013). The Frieze pattern has a unique feature always created by translation (Rahmawati et al., 2018). The frieze pattern is a discrete group belonging to the plane symmetry group, a subgroup of isomorphic translations (Gallian, 2021). The symmetries formed in the frieze pattern consist of translation, rotation, reflection, or glide reflection. The Frieze pattern creates seven different patterns. The seven patterns are Pattern 1 only experiences translation in one direction; Pattern 2 has one-way translation and glide reflection; Pattern 3 has one-way translation and vertical reflection; Pattern 4 undergoes one-way translation, and there is a 180° rotation; Pattern 5 has one-way translation, rotation, vertical reflection, and glide reflection; Pattern 6 experiences one-way translation and horizontal reflection; and Pattern 7 undergoes one-way translation, rotation, vertical and horizontal reflection. While the crystallographic pattern is a flat pattern in a two-dimensional plane that forms a grid. In the crystallographic pattern there are 5 types of unit grid namely square, parallelogram, rhombus, and hexagonal where the two-dimensional plane has four types of symmetry namely translation, reflection, rotation, and shear reflection (Liu & Collins, 1998). Patterns formed in flat shapes that are contained in woven cloth motifs like this can be used in learning mathematics.
This classification has several notations, including 1) The letters \( p \) and \( c \) denote primitive cells (unit grid) or centered cells. In general, primitive cells have centers with the highest rotational order located at grid points, while centralized cells have a reflection axis that is vertical to one or two sides of the cell; 2) An integer \( n \) indicates a high order or turnover rate; 3) The symbols indicating that the axis of symmetry is vertical to the \( x \)-axis of the cell (i.e., the left side of the cell) are \( m \) (mirror) denoting the reflection axis, \( g \) indicates no reflection but the glide reflection axis; and 4) A symbol denoting an axis of symmetry at an angle \( \alpha \) to the \( x \)-axis, with \( \alpha \) depending on \( n \), the highest order or degree of rotation: \( \alpha = 180^{\circ} \) for \( n = 1 \) or \( n = 2 \), \( \alpha = 45^{\circ} \) for \( n = 4 \), \( \alpha = 60^{\circ} \) for \( n = 3 \) or \( n = 6 \).

Mathematics learning becomes more meaningful by constructing knowledge, involving culture through artifacts and students' everyday experiences as basic knowledge (Bonotto, 2017; Halini, et al., 2023). In addition to utilizing the right artifacts, the teaching and learning environment is also designed according to student culture and implemented into mathematics learning activities through new socio-mathematics norms (Bonotto, 2017). Ethnomathematics provides an opportunity to connect mathematics with culture. Ethnomathematics applications can be found in the environment where children grow and develop (D'Ambrusio & Rosa, 2016; Nuqthy, Nityana, & Navia, 2022). Ethnomathematics can be defined from its pedagogical aspect, namely the relationship between mathematics content and student culture (Amit & Qouder, 2017; Meilina, Mariana, & Rahmawati, 2023). However, most mathematics learning in schools does not involve culture in exploring students' initial knowledge obtained from their environment. This is because the teacher's teaching is formal, only presenting the material in abstract mathematics. This study aims to find frieze patterns, crystallographic patterns, and philosophical values in subahnale woven fabric motifs in Sukarare Village, which can be used as a source of learning mathematics in Lombok. In addition, the independent curriculum currently being developed emphasizes that learning must integrate each learning content with culture and everyday life, especially in the form of local wisdom.
II. METHOD

The research method used in this study is the ethnographic method, which examines and describes a society's culture. (Spradley, 2016). This research method was chosen because it is consistent with the goals of ethnomathematics, which is to study mathematical ideas, processes, and techniques in culture from a societal perspective. The interpretation of phenomena in the ethnographic method describes, analyzes, and interprets cultural group elements, such as patterns of behavior, beliefs, and language that develop over time. (Spradley, 2016).

Subahnale woven fabric artisans on the island of Lombok create different motifs and names. Data collection was carried out by field surveys and interviews with specially selected informants. The procedure for choosing informants was conducted to determine the criteria for informants according to the data to be collected. The source person was Lalu Damsiah, a traditional figure from Sukarara Village, Central Lombok, who was used as an informant to find comprehensive information on the origins of subahnale woven fabrics in Sukarara Village. Mrs. Manggis, a songket woven fabric maker in Sukarara Village, was used as an informant in comprehensively exploring the meaning of the symbols and forms of subahnale woven fabric motifs in Sukarara Village. Mr. Gesum, a traditional figure from Sukarara Village, was used as an informant to find comprehensive information about the development of subahnale woven fabrics. Inaq Umi, a subahnale cloth weaver in Sukarara Village, was used as an informant to find complete details about the shape and meaning of each woven cloth motif. Lalu Agus Fathurrahman, a Sasak humanist, was used as an informant to find information about the philosophy and cultural importance of symbols on traditional Sasak woven cloth, and Moch Yamin, a West Nusa Tenggara humanist, was used as an informant to find comprehensive information about the philosophy and symbolic meanings of motifs from cloth Subahnale weaving.

To complement the results of observations and interviews, researchers conducted a literature review on subahnale woven fabrics. The data collection results were analyzed using a triangulation technique to comprehensively explore the relationship between the mathematical knowledge system in the form of frieze patterns and crystallographic patterns with the philosophical values contained in other subahnale weaving motifs. The data collected is then reduced by data reduction to select raw data, simplify, abstract, and transform field data. After data reduction, the next step is data presentation, namely data separation based on content so that conclusions can be drawn later.

III. RESULT AND DISCUSSION

Weaving or nyensek is a hereditary tradition passed down by the ancestors of
the Sasak people from generation to generation. Activities nyensek carried out by women take advantage of the rest time on the sidelines of farming activities. The resulting woven fabric motifs are pretty diverse. The motifs show not only sheer beauty but every motif contained has a philosophical meaning. Many types of subahnale woven fabric motifs have been developed. Apart from being used as daily clothing, the woven cloth produced is also used in traditional activities and rituals designed by the Sasak people.

The motif or reragian subahnale woven fabric in Sukarara Village is formed from geometric patterns such as rectangles, squares, and triangles. The resulting design is determined when cutting the pakan using traditional tools. A geometric pattern is formed from the crossing of pakan and twine lungsin. Pakan thread is a thread that is arranged in the same direction as the length of the cloth, while the lungsin thread is a thread that follows the width of the fabric.

Subahnale woven cloth did not have a parian, but in its development, subahnale woven fabric made motifs (reragian) with names depending on the shape of the motif. There are many subahnale woven fabric motifs, including the wayang motif, the keker motif, the serat penginang motif, the bulan bekurung motif, and the bintang empat motif.

Subahnale woven fabric is one of the fabrics that has existed since the reign of Datu Panji Sukarare and Dende Terong Kuning. This cloth has a geometric motif with a lotus flower decoration inside. Taking the lotus flower as a motif symbolizes prosperity. The edge of the fabric is also decorated with many patterns that combine many forms.

The primary colors used are dark colors such as blue, maroon, and black. The color of the motif uses contrasting colors such as white, light blue, or bright yellow. A noble daughter did this woven cloth with various rituals and special conditions for quite a long time. After the fabric was finished, it was shown to the public. The whole community was amazed by the material's beauty and said Subhanallah, so in the end, the cloth was named subahnale.

A. Subahnale woven fabric pattern

Woven fabric subahnale is a songket cloth with the highest level of complexity. That said, not everyone can weave this type of songket. Only people of blue blood or nobility can weave songket subahnale (Damsiah, 2022). If someone not belonging to the nobility class incorporates this type of songket, he will fall ill. This is because the people of Sukarara Village still believe that songket weaving is sacred. This subahnale songket is a very famous songket. Not only the level of complexity during the manufacturing process, but the aesthetic beauty both in terms of motifs and colors has made this subahnale songket cloth has its charm. In addition, songket subahnale also has a meaning related to the spiritual and sacred world.
The motif on the top of the *subahnale woven cloth* is decorated with a series of lotus flower motifs which symbolize fertility and prosperity. These motifs are arranged neatly in the same pattern and shape using gold thread.

Figure 3 above shows that the primary form of the subahnale woven fabric motif at the top is a geometric shape, namely a rhombus and a hexagon.

Figure 4 above shows that the motifs arranged on the *subahnale woven fabric* use the concept of geometric transformation, namely reflection, where the motif is reflected on the Y axis.

As shown in the picture above, the top motif of the subahnale woven fabric has vertical reflections but no horizontal reflections. Furthermore, based on the flowchart, it can be seen that the pattern has half turns. So, the geometric pattern in the motif on the *subahnale woven fabric* is pattern 6: experiencing one-way translation and horizontal reflection.

Figure 5. The motif in the middle of the *subahnale woven fabric*

The motif pattern shown in Figure 5 of the *subahnale woven cloth*, the middle part is a hexagon shape with a lotus flower in it. Geometry shapes also look like rhombuses, triangles, and squares that fill any empty spaces in the same direction.

Figure 6. Basic sketch of the motif for the middle part of the *subahnale woven fabric*

Figure 6. above shows that this pattern has a rhombus lattice and a rotation of 90°. In addition, there are 4-way reflections. So, the crystallography found is a p4m pattern. Besides that, the motif in the middle of the *subahnale woven fabric* is part of the lotus flower motif. The design has a rhombus and hexagonal lattice but not the smallest degree of rotation, nor does it have reflection and glide reflection. So, in this pattern, we found a crystallographic p1 way.
**Subahnale** motif pattern There is a one-way translation with a 180° rotation and a horizontal reflection. So, pattern four is found in the freeze pattern.

![Pattern Figure](image.png)

**Figure 8. Reflection of subahnale woven fabric motifs**

Figure 8 above shows reflections on both axes on the x-axis and y-axis, experiencing one-way translation, rotation, and vertical and horizontal reflection. The pattern found is pattern 7 in the frieze pattern.

![Motif Figure](image.png)

**Figure 9. The motif of the subahnale woven fabric**

The pattern on the bottom of the *subahnale woven fabric* is a triangular shape that repeats itself in the long direction of the material. The motif used is the motif of the lotus flower shape.

![Sketch Figure](image.png)

**Figure 10. Basic sketch of the motif on the bottom of the subahnale woven fabric**

Figure 10 above shows the pattern of the *subahnale woven fabric motif* at the bottom. It can be seen that the pattern only has vertical reflections and also does not have a 180° rotation. So, the bottom pattern of the *subahnale woven fabric* can be categorized as pattern 3 in the Frieze pattern.

### B. Philosophical Values

* A noblewoman makes *subahnale woven fabric* with a unique selection of materials and colors, which takes a long time to make (Damsiah, 2022). Furthermore, at that time, there was not much production of woven cloth because it was only used by certain people (Gesum, 2022). The philosophical values contained in *subahnale* woven fabric motifs are as follows:

#### Table 1. The philosophical values contained in *subahnale* woven fabric motifs

<table>
<thead>
<tr>
<th>Dimensions</th>
<th>Philosophical value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Black base color</td>
<td>Most of the primary colors of woven fabrics, traditional clothing, and other accessories from the Sasak people are black (dark). This is taken because black is a neutral color, reflecting togetherness, strength, and courage (Damsiah, 2022)</td>
</tr>
<tr>
<td>Triangle</td>
<td>According to the Sasak people, the triangular symbol is the alignment of three elements: the relationship between humans and nature, humans and humans, and humans and God.</td>
</tr>
<tr>
<td>Rectangular</td>
<td>The quadrilateral consists of three directions. To realize the prosperity of a nation, it must synergize between four components, namely pandite (government), nyake (scholars/intellectual), guru (religious leaders), and kire (people) (Fathurrahman, 2022)</td>
</tr>
<tr>
<td>Hexagon</td>
<td>The form of belief in Islam is the pillars of faith (Fathurrahman, 2022)</td>
</tr>
</tbody>
</table>
Based on the philosophical values of the colors and shapes of the motifs contained in the subahnale woven fabric above, it gives a meaning that can be used as part of advice and as a lifeline for the next generation.

**IV. CONCLUSION**

Subahnale woven fabric is the oldest woven fabric in Sukarare Village. The motifs and colors of the threads that adorn this woven fabric, besides having an aesthetic meaning and containing philosophical values, can also be used as a source of learning mathematics. Various geometric shapes adorn this subahnale woven fabric, including hexagons, triangles, squares, and rhombuses. The figures are placed based on geometric transformation patterns: translation, rotation, and reflection. This study has observed ethnomathematics elements of subahnale woven fabric motifs based on Frieze and Crystallography patterns and analyzed Frieze patterns or Crystallographic patterns in one woven fabric pattern. These patterns are found by cutting the motifs vertically and horizontally and then rotating them to find Frieze or Crystallographic ways. The study found that there were 4 Frieze patterns in subahnale woven fabric motifs. The Frieze patterns are patterns 3, 4, 6, and 7. In addition, there are also crystallographic patterns. The crystallographic ways are p1, pm, and p4m patterns. Subahnale woven fabric motifs are the result of development. The variant name of the woven fabric depends on the form of the motif used. These variants include subahnale woven fabric with wayang motifs, subahnale woven fabrics with nanas motifs, subahnale woven fabrics with benang empat motifs, etc. For this reason, it is suggested that future researchers export forms of mathematics through ethnomathematics studies to make the sources of learning mathematics more culturally related.

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**AUTHORS’ BIOGRAPHY**

**Dr. Lalu Muhammad Fauzi, M.Pd.Si.**

Born in Suralaga, 12 February 1973. Teaching staff at Hamzanwadi University. Undergraduate study, Mathematics Education Study Program at STKIP Hamzanwadi Selong, graduated in 2006; Masters in Mathematics Education, Universitas Negeri Yogyakarta, graduated in 2010; and Doctoral Degree in Mathematics Education, Universitas Negeri Yogyakarta, graduating in 2021.

**Dr. Shahibul Ahyan, M.Pd.**


**Dr. Sri Supiyati, M.Pd.Si.**

Born in East Lombok, 2 April 1979. Teaching staff at Hamzanwadi University. Bachelor of Mathematics Education STKIP Hamzanwadi Selong, (Selong), graduated in 2001; S2 (Mathematics Education, Universitas Negeri Yogyakarta), (Yogyakarta), graduated in 2010; and S3 Mathematics Education Consulate (Universitas Negeri Yogyakarta), (Yogyakarta), graduated in 2019.

**Nila Hayati, M.Pd.**

Born in Masbagik, March 21, 1988. Teaching staff at the Mathematics Education Study Program, Hamzanwadi University, received a Bachelor of Mathematics Education from Institut Agama Islam Negeri Mataram (2010) and a Masters in Educational Research and Evaluation from Universitas Negeri Yogyakarta (2013).

**Rody Satriawan, M.Pd.**